Statistical CSI: An Attempt to Detect Fraud in Papers Published From a Medical Biochemistry Department

Mark Hudes, PhD Senior Statistician Children's Hospital Oakland

Assumption:

The observed data are normally distributed with finite mean μ and finite variance σ^2 .

The population CV (expressed below as a proportion), CV_{pop} , would then be

 $CV_{pop} = \sigma/\mu$.

This is estimated by the sample CV,

$$CV_{sample} = s/\overline{x}$$

where $\overline{\mathbf{x}}$ and s are the sample mean and sample sd.

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For a sample of size n from a normal distribution,

$$T = \sqrt{n}/CV_{m}$$

has a noncentral Student t distribution with n -1 degrees of freedom and noncentrality parameter

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 $ncp = \sqrt{n}/CV_{m}$

$$\begin{split} \hline \text{Construction of Boundaries Within Which 50% of CVs} \\ & \text{Are Likely to Fall} \\ \\ & P(t_{0.25}' < T < t_{0.75}') = 0.50 \\ & P\left[\frac{1}{t_{0.25}'} < \frac{\text{CV}_{\text{sample}}}{\sqrt{n}} > \frac{1}{t_{0.75}'}\right] = 0.50 \\ & P\left[\frac{\sqrt{n}}{t_{0.75}'} < \text{CV}_{\text{sample}} < \frac{\sqrt{n}}{t_{0.25}'}\right] = 0.50 \\ & \text{Hudes ML et al 2008 Faseb J23:689-703 (2009)} \end{split}$$

The median CV from each journal article was used to estimate $\text{CV}_{\text{pop}}.$

The construction of these intervals makes the following assumptions:

- All measurements are on the same variable, such as a particular enzyme activity;
- All measurements are from the same treatment group, such as the control group or a group treated with lipoic acid;
- c) The median CV is an adequate estimate of CVpop.
- d) Each variable being examined has an approximate normal distribution.

Calculation of an approximate "P value"

The binomial distribution was used to compute the likelihood of obtaining k or more (out of a total of N) CVs **inside** the constructed 50% limits.











